

The influence of collective behaviour on pacing in endurance competitions

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Keywords

decision-making, endurance performance, complex systems, Sport, Mental Fatigue

Abstract

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A number of theoretical models have been proposed to explain pacing strategies in individual competitive endurance events. These have typically related to internal regulatory processes informing the making of decisions relating to muscular work rate. Despite a substantial body of research investigating the influence of collective group dynamics on individual behaviours in various animal species, this issue has not been comprehensively studied in individual athletic events. This is surprising given that athletes directly compete in close proximity to one another, and that collective behaviour has also been observed in other human environments. Whilst reasons for adopting collective behaviour are not fully understood, it is thought to result from individual agents following simple local rules resulting in seemingly complex large systems acting to confer some biological advantage to the collective as a whole. Although such collective behaviours may generally be beneficial, endurance events are complicated by the fact that increasing levels of physiological disruption as activity progresses may compromise the ability of individuals to continue to interact with other group members. This could result in early fatigue and relative underperformance due to suboptimal utilisation of physiological resources by some athletes. Alternatively, engagement with a collective behaviour may benefit all due to a reduction in the complexity of decisions to be made and a subsequent reduction in cognitive loading and mental fatigue. This paper seeks evidence for collective behaviour in previously published analyses of pacing behaviour and proposes mechanisms through which it could potentially be either beneficial, or detrimental to individual performance.

Ethics statement

(Authors are required to state the ethical considerations of their study in the manuscript including for cases where the study was exempt from ethical approval procedures.)

Did the study presented in the manuscript involve human or animal subjects: No

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13 Keywords: decision-making, endurance performance, complex systems, sport

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15 Abstract

A number of theoretical models have been proposed in recent years to explain pacing 16 strategies observed in individual competitive endurance events. These have typically related 17 18 to the internal regulatory processes that inform the making of decisions relating to muscular 19 work rate. Despite a substantial body of research which has investigated the influence of collective group dynamics on individual behaviours in various animal species, this issue has 20 21 not been comprehensively studied in individual athletic events. This is somewhat surprising given that athletes often directly compete in close proximity to one another, and that 22 collective behaviour has also been observed in other human environments including 23 pedestrian interactions and financial market trading. Whilst the reasons for adopting 24 collective behaviour are not fully understood, collective behaviour is thought to result from 25 individual agents following simple local rules that result in seemingly complex large systems 26 that act to confer some biological advantage to the collective as a whole. Although such 27 collective behaviours may generally be beneficial, competitive endurance events are 28 complicated by the fact that increasing levels of physiological disruption as activity 29 progresses may compromise the ability of some individuals to continue to interact with other 30 31 group members. This could result in early fatigue and relative underperformance due to suboptimal utilisation of physiological resources by some athletes. Alternatively, engagement 32 with a collective behaviour may benefit all due to a reduction in the complexity of decisions 33 34 to be made and a subsequent reduction in cognitive loading and mental fatigue. This paper 35 seeks evidence for collective behaviour in previously published analyses of pacing behaviour and proposes mechanisms through which it could potentially be either beneficial, or 36 detrimental to individual performance. It concludes with suggestions for future research to 37 enhance understanding of this phenomenon. 38

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44 **1. Introduction**

'Pacing' is the term used to describe the distribution of muscular work rate throughout an 45 exercise bout, and is a fundamental requirement of successful endurance performance (Foster 46 et al., 1994). A great deal of published research in recent years has investigated the regulatory 47 mechanisms that allow effective regulation of pacing to be achieved. Although there appears 48 to be little consensus in the literature with regards to the precise processes involved, the 49 50 momentary Rating of Perceived Exertion (Tucker, 2009), the Hazard Score (DeKoning et al., 2011), and emotion (Baron et al., 2011, Renfree et al., 2012) have all been suggested to be 51 contributing factors. More recently Smits et al., (2014) and Renfree et al., (2014) have 52 53 identified the need for greater consideration of decision-making processes in explaining observed athletic behaviours. Again, whilst the precise processes remain unclear, several 54 potential models have been proposed for further investigation. It is apparent, however that 55 whilst considerable research effort has been invested in enhancing understanding of decision-56 making based on internal regulatory processes (Tucker, 2009; Marcora & Staiano, 2010; De 57 Koning et al., 2011; Smits et al., 2014), less has been placed on the possible influence of 58 external factors such as the relative presence, or indeed absence of other competitors. 59 Collective behaviours have been described in a number of non-biological, animal and human 60 environments, and can be explained by relatively simple laws governing interactions being 61 followed by individual agents giving rise to complex large systems. The aim of this paper is 62 to identify the possible mechanisms through which the presence of other competitors might 63 influence collective group behaviour and therefore individual pacing decisions, and to 64 propose future research priorities. 65

66 **2. Collective behaviour**

A key feature of most individual competitive endurance events is that athletes race directly 67 68 against other competitors, sometimes in individually marked lanes, and at other times within closer proximity to one another. This may mean that adopted behaviours are heavily 69 70 influenced by those displayed by other nearby individuals, a phenomenon that has been studied extensively in other human and animal models. For example, so called 'herd 71 behaviour' (Bannerjee, 1992) has been found to occur in numerous situations. The model of 72 73 herd behaviour suggests that in complex decision-making environments, the 'easiest' decision to make is simply to do exactly the same as those who happen to be in close 74 proximity, or at least those of whom the individual is aware. Complex systems theory 75 76 suggests that through individual agents following very simple local rules governing 77 interactions, it is possible to generate large, seemingly complex patterns characteristic of biological systems (Wolfram, 1985). Through mathematical modelling, it has been 78 demonstrated that individual agents following relatively simple rules can explain the 79 collective motion (using terms such as swarms, schools, flocks, herds, and murmurations) of 80 various animal species (King and Sumpter, 2012). A key feature of all these collective 81 behaviours is that they emerge in the absence of any obvious centralised control, but rather 82 83 because some localised information originating from neighbours flows through a system and results in the production of a collective pattern (Giardina, 2008). Although the precise 84 reasons for the adoption of such behaviours are unknown, it is thought that they may aid in 85 the avoidance of predation, or else be a mechanism through which useful information, such as 86 87 location of food sources, may be conveyed between group members (King and Sumpter, 2012). Herd behaviour has also been displayed by humans in various environments. For 88 89 example, in financial markets individual market participants appear to mimic one another,

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90 leading to heavy tails in the distribution of stock price variations (Cont and Bouchard, 2000),

- 91 whereas self-organising phenomena would appear to explain the 'flow' behaviour of
- 92 pedestrians (Helbing et al., 2005), whereby the time gap between individuals is influenced by
- boundary conditions in corridors and at intersections. This tendency towards collective
- behaviour and group formation appears to be based on a collective group memory, whereby
- 95 previous history of group structure influences future collective behaviours, and individuals
- 96 learn to change spatial positions within a group based on adoption of local 'rules of thumb'
- 97 (Couzin et al., 2002).

98 Interestingly, collective behaviour appears to not only occur in biological systems.

99 Experimental work by Giomi et al. (2013) demonstrated that brainless 'bristle-bots'

100 (constructed from toothbrush bristles and an on-board cell phone vibrator motor) transitioned101 to collective swarming and swirling behaviour when confined to a limited area. This finding

102 may suggest that the formation of collective behaviours is a spontaneous occurrence that

translates into swarm intelligence. However, it must be acknowledged that while many

analyses of collective behaviours have tended to treat individuals as simple interacting

105 physical units (Giordana, 2015), there are potential limitations to this approach. Specifically,

106 in biological systems individual behaviours may well derive from complicated biological

107 processes rather than simple physical laws. Indeed, and in relation to athletic activity, Smits

108 et al (2014) suggest that in order to fully explain decisions related to pacing in athletic events,

109 it is necessary to understand how perception and action are coupled in determining behaviour,

110 therefore suggesting an ecological approach may be required.

111 **3.** Collective behaviour in sport

At this point it should be emphasised that competitive sporting events differ from most other 112 human and animal environments in a key respect. Whilst the possible reasons for such 113 behaviour identified earlier, including avoidance of predation and the sharing of information 114 relating to the location of food (King and Sumpter 2012), may be expected to benefit the 115 collective as a whole, in individual endurance events it would seem implausible that 116 individuals would consciously adopt behaviours that would benefit other rival competitors. 117 Competitive sporting events may therefore be considered rather artificial environments from 118 a biological perspective, and the influence of engagement in collective behaviours warrants 119 investigation. Given the complexity of the internal biological processes and the interactions 120 between autonomous biological entities, identification of simple rules governing both 121 individual and collective behaviour in sport environments may be impossible. However, to 122 our knowledge no study has attempted to identify relative weightings given to external and 123 internal processes in determining decisions made relating to muscular work rate during 124 125 individual competitive endurance events.

126 Although some research has suggested that sports teams should be considered

127 'superorganisms' whose behaviour results from collective processes (Duarte et al, 2012), less

research is available relating to collective behaviour in self-paced endurance activities.

129 Undoubtedly any behaviour displayed in such an environment would be complicated by the

fact that performance capacity would be disrupted to a greater or lesser extent as an eventprogressed due to increasing physiological disruption. A financial trader or a pedestrian can

132 'follow the herd' for long periods of time with few biological consequences, whereas a

133 competitor in an endurance race may initially be able to do so before finding their ability to

134 continue is compromised through metabolic disturbance. Indeed, in racing cyclists Trenchard

et al., (2014) suggest a peloton exhibits collective behaviour similar to that displayed by

136 flocking birds or schooling fish. A number of general processes were proposed that explained

the formation of large collectives and the separation of individuals or sub-groups from these during mass start velodrome races. These behaviours may reflect inherent evolved processes that maximise energy savings during collective activities. In a very recent paper, Trenchard (2015) goes on to suggest that cyclists display 'protocoperative' behaviour whereby they engage in cooperative activity. However, once the power outputs required for engaging in this activity become prohibitive due to continued physiological disruption, athletes can no longer cooperate, and eventually they become uncoupled from the peloton.

The issue of energy savings in cyclists described above may imply that collective behaviour 144 would be beneficial in endurance sports such as this where speeds are high. Indeed, a paper 145 by Kyle (1979) suggests that 80-90% of the metabolic cost of cycling is accounted for by the 146 overcoming of wind resistance, but that cycling in a group reduced power output required at 147 typical racing speeds by 30%. Trenchard (2010) later suggested that the formation of the 148 peloton, characteristic of cycle road races, is actually formed in order to maximise collective 149 energy expenditure. During running, where speeds are considerably lower, Kyle (1979) found 150 only 4-8% of total energetic expenditure was utilised in the overcoming of wind resistance, 151 and this was reduced by just 2-4% when running in a group. If collective behaviour is an 152 evolved characteristic that informs decision-making in a group environments, then we 153 propose that such behaviour may indeed be detrimental to athletic performance in some 154 sporting events (such as running races) in which high performance is not generally associated 155 with any survival advantage (which would be the driver of evolved behaviours). In order to 156 better understand the influence of collective behaviour on pacing strategy then, it is necessary 157 158 to seek evidence for this occurring in running events where it should be less advantageous from a physiological perspective. 159

160 **4. Evidence for collective behaviour in competitive endurance events**

There already exists some evidence for collective behaviours informing decisions relating to 161 pacing during endurance events. In elite runners competing in both the World Cross Country 162 Championships (Esteve Lanao et al., 2014; Hanley, 2014) and the World Marathon 163 Championship (Renfree & St Clair Gibson, 2013), a common observation was made in that 164 all runners adopted similar absolute running speeds early in the races, but that runners who 165 eventually finished behind the leading athletes progressively decelerated. This resulted in 166 overall 'positive' pacing strategies for the majority of athletes which are characterised by a 167 second half completed at a slower speed than the first. Such strategies are typically 168 considered suboptimal for events of this kind of duration (Abbiss & Laursen, 2008). In our 169 analysis of the World Championship marathon race (Renfree & St Clair Gibson, 2013) we 170 found the degree of underperformance depended on the athlete's absolute performance 171 172 potential as determined by their personal best times over the distance. When all athletes were split into quartiles based on their eventual finishing position, it was not surprisingly found 173 that mean personal best speeds of each quartile decreased from the leading athletes to those 174 who finished towards the rear of the race. However, the degree of 'underperformance' 175 relative to personal best times also increased as athletes finished further behind the leaders. 176 177 This would suggest that the adoption of collective behaviours (i.e. similar starting speeds) at the outset of the race had greater negative effects on the athletes with lower absolute 178 performance capacities. Although no measures of physiological responses are available for 179 this event, it can be speculated that physiological disruption would be greater in those athletes 180 181 of lower performance capacity, and that therefore the degree of underperformance in the latter stages of the race would be greater. This disruption and underperformance may also be 182 expected to result in higher ratings of perceived exertion and more negative affective 183 responses. This may explain the findings by Mytton et al., (2015) who demonstrated that 184

185 medal winning athletes in international running and swimming events displayed greater increases in speed in the final stages than non-medal winning athletes. This greater 186 acceleration in pace would be possible as a result of the possession of a greater metabolic 187 reserve capacity (Swart et al., 2009) in the superior athletes. Konings et al. (2015) also 188 demonstrated very similar findings in 1500m short track speed skaters, whereby 'top' 189 finishers were only faster than 'bottom' finishers in the final 5 laps (out of 13.5) in elite level 190 191 competitions. However, speed skating races are completed at higher speeds than running events of the same distance meaning that energy savings from collective behaviour would be 192 expected to be greater. Despite this, Konings et al. (2015) also found that tactical positioning 193 194 during the latter stages of the race was a strong determinant of final finishing position. In this case then, it may be that the energetic costs of accelerating and overtaking leading athletes 195 (and thereby skating further on the bends) may prohibit the gaining of positions when overall 196 speeds are high, even though there may be benefits in avoiding leading earlier in the race. 197 This example again emphasises the importance of consideration of the behaviour of other 198 group members on explaining individual behaviours during competitive endurance events. 199

5. Potential influence of collective behaviour on mental fatigue

Although the above may suggest that collective behaviours may ultimately be detrimental to 201 some individual athletes during events such as running races, it should be acknowledged that 202 there are also potential benefits. Zouhal et al. (2015) found that drafting behind another 203 runner improved 3000m running performance without any reduction in energy expenditure or 204 205 cardiovascular effort, leading the authors to propose that a pacemaker may act to improve performance through psychological mechanisms. It should however, be acknowledged that 206 the data presented in this paper could also be interpreted in a different manner. An increased 207 208 running speed at the same level of cardiovascular effort could also imply participants benefitted from an energy saving provided by drafting. Given that regulation of pace requires 209 continual decision-making (Smits et al., 2014: Renfree et al., 2014), it may therefore be 210 211 suggested that following another athlete may act by reducing the number of decisions to be made, and therefore decrease cognitive loading. Vohs et al. (2014) have established that the 212 process of decision-making leads to a subsequent loss of self-control characterised by, 213 amongst other things, reduced physical stamina and reduced persistence in the face of failure. 214 Indeed, mental fatigue can be induced by prolonged periods of cognitive activity, and is 215 associated with impaired exercise tolerance despite it not influencing cardiorespiratory or 216 217 metabolic factors (Marcora et al., 2009). Some support for this suggestion that group membership may be beneficial in endurance events is provided by Hanley (2015) who 218 analysed pack running in the IAAF World half marathon championships. Those athletes who 219 ran in packs throughout the race showed smaller decrements in speed than those who did not 220 do so, or did so only for parts of the race. Those athletes who did run in packs throughout 221 also demonstrated greater accelerations in pace in the final stages, suggesting either 222 maintenance of a greater metabolic reserve capacity, or that they had developed lower levels 223 224 of mental fatigue. Hanley (2015) went on to suggest that in order to optimise performance, athletes should identify likely rivals of similar performance capacity in advance of the race 225 and then aim to run with them as part of their pre-race strategy. There is as yet, however, no 226 evidence that this is actually a good strategy. If running as part of group is to be effective in 227 maximising endurance performance, its success or otherwise may therefore depend on the 228 ability to accurately self-assess performance capacity and also that of other athletes. Any 229 230 mismatch between individual physiological capacity and that of the group as a whole will lead to incomplete realisation of performance capacity 231

In contrast to endurance running races whereby athletes compete directly and in close 232 proximity to one another, pool based swimming races are completed with athletes in their 233 own individual lanes, meaning that collective behaviours are impossible. In swimming races 234 pacing profiles are consistent between competitions, and elite athletes do not appear to vary 235 their tactics or modify their pacing strategies between events (Skorski et al., 2014). Earlier 236 work by Skorski et al., (2013) had also demonstrated that swimmers produced faster times in 237 238 real than simulated competitions, and that these faster times were achieved through swimming faster in each intermediate stage rather than adoption of a different overall 239 strategy. These observations may suggest that when athletes are isolated from their direct 240 241 competitors as a result of swimming in their own lane, then the reduced opportunities to engage in collective behaviour means there is less variation in pacing displayed by athletes of 242

243 differing performance levels competing in the same event.

6. Future perspectives

We have proposed that the human tendency towards collective behaviours may go some way 245 to explaining pacing decisions displayed by competitive athletes in some athletic events. 246 However, athletic events are rather 'artificial' from a biological perspective, and therefore the 247 effects of engagement in such behaviours are uncertain. Although this tendency may be 248 advantageous in relatively high speed endurance sports whereby energy savings from drafting 249 are significant (for example cycling), it may actually be detrimental in lower speed activities. 250 Athletes with inferior physiological capacities will be unable to maintain work-rates set by 251 superior athletes and consequently suffer both physiological and psychological perturbations. 252 Indeed, although there is some evidence that athletes in running events of relatively long 253 duration (cross country and marathon running) may select starting speeds based on those 254 255 selected by other competitors, it may be hypothesised that the relative benefit of engagement in such collective behaviour may be greater in shorter running events whereby potential 256 energetic savings from drafting are increased. This could result in greater group density, or 257 258 slower athletes maintaining contact with faster athletes for a greater fraction of total race distance. It may also be the case that collective behaviour is less evident in sports where there 259 is greater separation between athletes in space or else they are to some extent isolated from 260 one another (for example through competing in their own lanes). Alternatively, it may be 261 possible that engagement in collective behaviours could be beneficial to performance through 262 reducing the requirement for continuous decision-making and a subsequent reduction in 263 mental fatigue, even in activities where energetic savings through drafting are minimal. 264

Further research is required in order to better understand the relative influence of both internal (physiological) and external (environmental) variables on decision-making regarding work rate during self-paced competitive, individual endurance activity. This could eventually lead to the development of strategies that allow athletes to make better pacing decisions that may optimise physiological capacity. Additional work is also required to increase understanding of sport specific tactical issues that will allow individual athletes to make

better pacing decisions that maximise their chances of optimising performance potential.

272 Author contributions

- AR: Devising and drafting the study, and revising it critically for the intellectual content
- 274 ECdC: Devising and revising the study critically for the intellectual content
- LM: Revising the study critically for intellectual content and final approval of the version tobe published.

DP: Revising the study critically for intellectual content and final approval of the version tobe published.

7. Conflict of interest statement

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